SOLUTIONS: FINAL EXAM, ECON302 (YELLOW)

Question 1 Let q be the probability that B chooses H. Then in order for A to be indifferent between H and T we must have 7q - (1 - q) = -q + (1 - q). Thus, q = 0.2. Thus,

Player A's expected payoff is 0.6

Question 2

(a) Then pure strategy Nash equilibria exist

If pure strategy equilibria exist, then mark which ones are equilibria (the first strategy listed is that of player A.



(b) Let p be the probability that B chooses Stag. In equilibrium A must be indifferent, i.e., 6p + 0(1 - p) = 5p + 3(1 - p). Solving this equation for p yields p = 3/4

In the mixed strategy equilibrium player A will hunt the stag with probability 3/4

Since the game is symmetric, PIayer B will hunt the stag with probability

Question 3

3/4



There is no pure strategy equilibrium. Let q be the probability that Joe chooses l. Then Rita must be indifferent between l and h, i.e., 10q + 25(1 - q) = 20q + 20(1 - q) = 20. Thus, q = 1/3.

If p is the probability that Rita chooses l then Joe must be indifferent, i.e., 10p + 10(1-p) = 5p + 20(1-p), i.e., p = 2/3.

Rita chooses low effort with probability 2/3Joe chooses low effort with probability 1/3Rita gets an A with probability 7/9 and a B with probability 2/9Joe gets an A with probability 2/9 and a B with probability 7/9

Question 4

(a) Let p be the cost of insurance. The expected utility from being insured is $\ln(120,000-p)$. For a low-risk person the expected utility from being uninsured is $0.98 \ln(120,000) + 0.02 \ln(20,000)$. Thus, $\ln(120,000-p) = 0.98 \ln(120,000) + 0.02 \ln(20,000)$.

Then a low-risk consumer's maximum willingness to pay for insurance

is **4,224.09**

For a high-risk person the expected utility from being uninsured is $0.6 \ln(120,000) + 0.4 \ln(20,000)$. Thus, $\ln(250,000-p) = 0.6 \ln(120,000) + 0.4 \ln(20,000)$.

A high-risk consumer's maximum willingness to pay for insurance is

$61,\!396.88$

The expected payment is 0.95 * 0.02 * 100,000 + 0.05 * 0.4 * 100,000. The price at which the insurance company would break even if they

insure both high and low risk consumers is **3,900**

Thus, **both types** will be insured).

(b) If a person has a pre-existing condition then this indicates that the person is a high-risk type. Thus, the expected cost is 40,000. Otherwise, the expected insurance payment is 0.99 * 2,000 + 0.01 * 40,000 = 2,380. Then the premium charged to a person with a pre-existing condition is

40,000

Then the premium charged to a person without a pre-existing condition

is **2,380**

Question 5 MC = 10. Thus,

$$10 = p\left(1 - \frac{2}{3}\right) = p/3.$$

the firm charges a price $p = 30$
the firm's profit/unit is 20
Now
$$10 = p\left(1 - \frac{1}{3}\right) = 2p/3.$$

the firm charges a price $p = 15$
the firm's profit/unit is 5

Question 6 The manager maximizes $0.05(100e - e^2) - 2e$. This expression is maximized when the derivative is 0, i.e., 5 - 0.1e - 2 = 0, which implies e = 30. The owner's profit is therefore $0.95(100e - e^2)$. Therefore,

If s = 0.05, the owner's payoff is 1,995

If s = 0.1 then the manager maximizes $0.1(100e - e^2) - 2e$. Again, this expression is maximized when the derivative is 0, i.e., 10 - 0.2e - 2 = 0, which implies e = 40.

If s = 0.1, the owner's payoff is 2,160

Question 7 The price elasticity of demand is $\epsilon = -0.1p/(10-0.1p) = p/(p-100)$. Thus,

$$20 = p\left(1 + \frac{p - 100}{p}\right) = p - 100 + p = -100 + 2p.$$

Thus, The profit maximizing price is 60

The firm sells 4 units

Revenue is 240. Cost are c(4) = 180. Thus,

The firm's profit is 60

Question 8

(a) The price elasticity of demand is $\epsilon_P = \frac{10p}{10p-1000} = \frac{p}{p-100}$. Marginal costs are 20. Thus, $20 = p\left(1 + \frac{p-100}{p}\right) = p + p - 100$. Thus,

The firm will charge a price p = 60

Demand is D(60) = 400. Thus, revenue is 24,000. Costs are c(400) = 13,000. Thus,

The firm's profit is 11,000

Individual demand is Q = y/100 = 400/100 = 4. Thus, an individual consumer spends 240 Dollars, which implies that m = 10,000 - 240 = 9,760. Thus, utility is u(4,9760) = 10,080.

A consumer's utility is 10,080

(b) Now marginal costs are 30. Thus, $30 = p\left(1 + \frac{p-100}{p}\right) = p + p - 100.$

The firm will charge a price p = 65

Demand is D(65) = 350. Thus, revenue is 22,750. Costs are c(350) = 15,500. Thus,

The firm's profit is now 7,250

The government's total tax revenue is 3,500

Individual demand is Q = y/100 = 350/100 = 3.5. Thus, an individual consumer spends 227.50 Dollars, which implies that m = 10,000 - 227.50 = 9,772.50. Thus, utility is u(4,9760) = 10,080.

A consumer's utility is 10,061.25

Thus, each consumer's utility loss is 18.75. Given that there 100 consumers, total loss is 1,875. The firm loses 3,750. The tax gain is 3,500. Thus,

The dead weight loss generated by the tax is 2,125

Thus, for each Dollar of taxes raised, the loss is 60.7 cents