

Name:

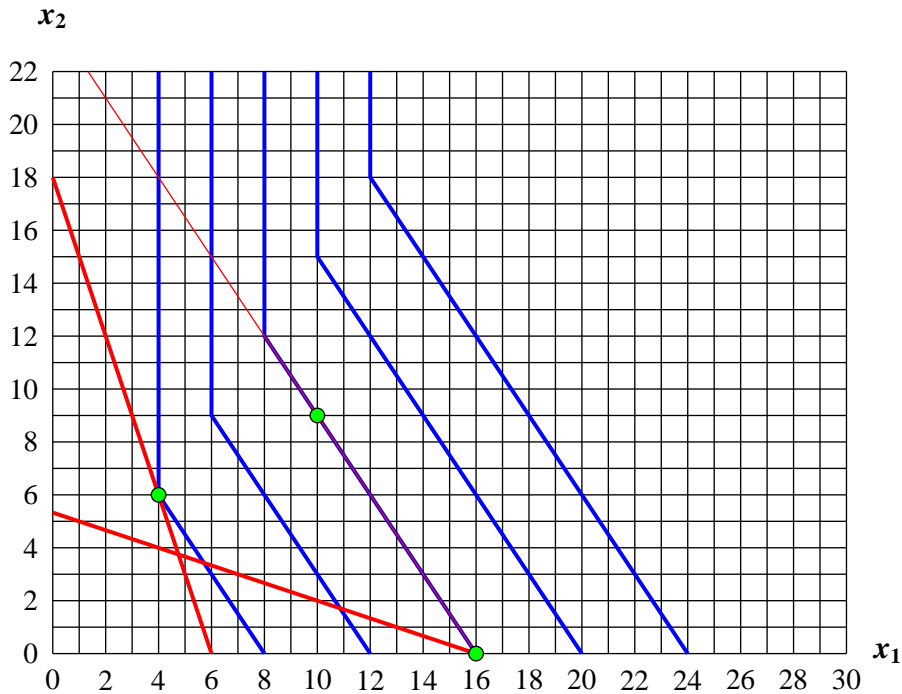
E-mail: @uiuc.edu

All questions must be answered on this test form!

For each question you must show your work and (or) provide a clear argument.

All graphs must be accurate to get credit.

Question 1 Consumer preferences are depicted below:



1. We must have $MRS = p_1/p_2$. Thus, $3/2 = p_1/30$, i.e., $p_1 = 45$.

Then $p_1 = 45, I = 720$.

2. If prices are $p_1 = 1, p_2 = 3$, then it is optimal only to consume good 1. Then the minimum amount of income the person needs to get the same utility as (8, 14) is given by $I = 16$.

3. If $p_1 = 3$ and $p_2 = 1$ and $I = 18$ then (4, 6) is optimal. Thus, the optimal consumption is $x_1 = 4, x_2 = 6$.

Question 2

- (a) $300 - 60 - 2P = 60 + P$. Thus, $P = 60$. Hence $Q = 120$

the government's tax revenue is 3,600

- (b) We get $300 - 60 - 2P = 60 + 30 + P$. Thus, $P = 50$ and $Q = 140$.

the government's tax revenue is 4,200

the government's total subsidy payments are 4,200

- (c) Demand is $Q_D(60) = 180$. Therefore $Q_S(60 + s) = 180$, i.e., $120 + s = 180$.
Thus, $s = 60$.

The subsidy is $s = 60$

Question 3

- (a) Let $Q_S(P) = a + bP$. Then $\epsilon_S = bP/Q$. Thus, $0.5 = 10b/100$. Hence, $b = 5$.
Thus, $100 = Q_D(10) = a + 50$. Hence, $a = 50$.

$Q_S(P) = 50 + 5P$

- (b) Suppose the demand function is given by $Q_D(P) = 20 - 4P$. Thus, $-1 = -4P/(20 - 4P)$, which implies $P = 2.5$

$P = 2.5$

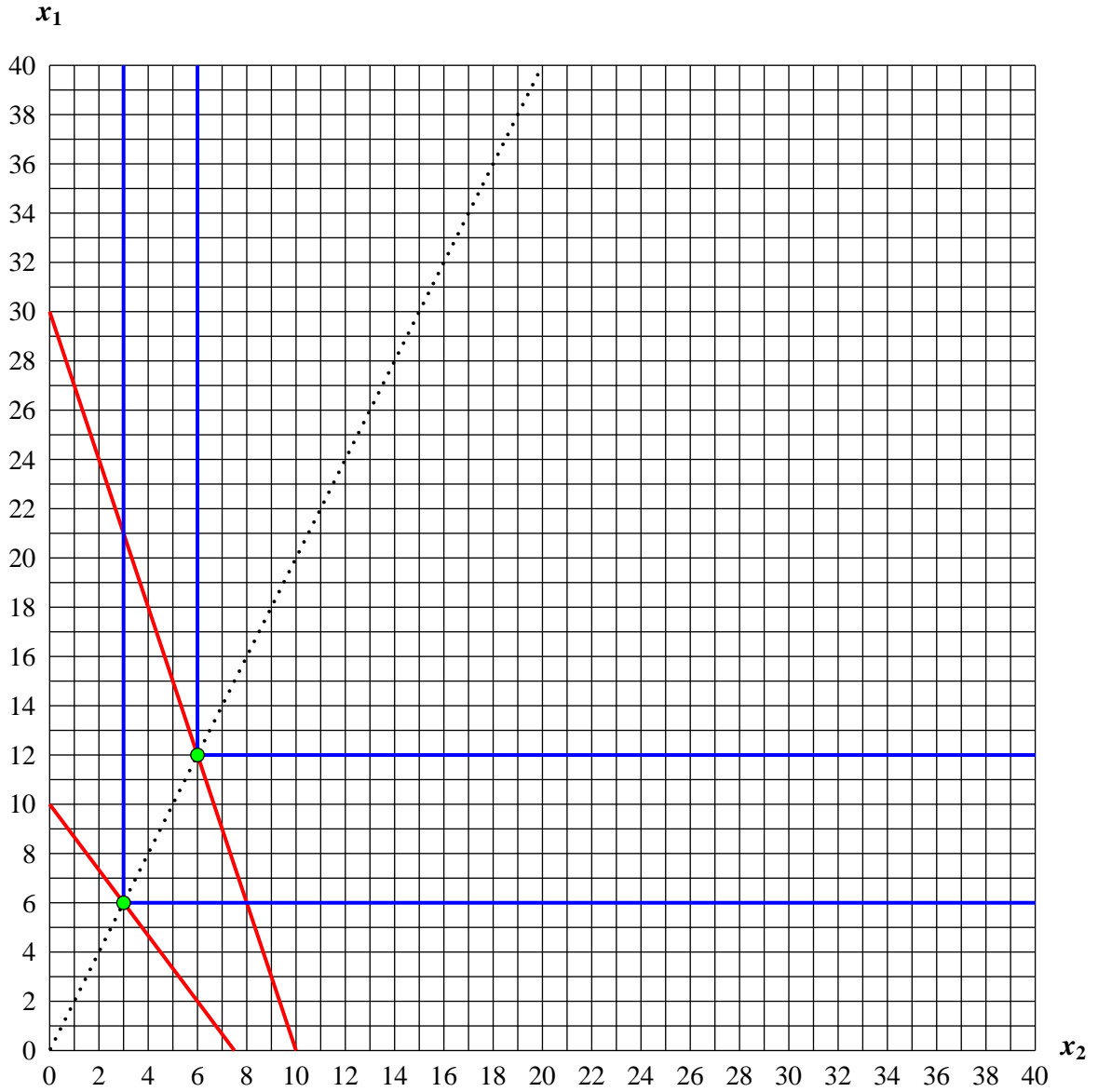
- (c) Let $Q_D(P) = a - bP$. Then $-30b/(a - 30b) = -1$, i.e., $a = 60b$. Further, at $P = 10$ demand is 100, i.e., $100 = a - 10b$. Hence $100 = 50b$, i.e., $b = 2$.
Thus,

$Q_D(P) = 120 - 2P$

Question 4

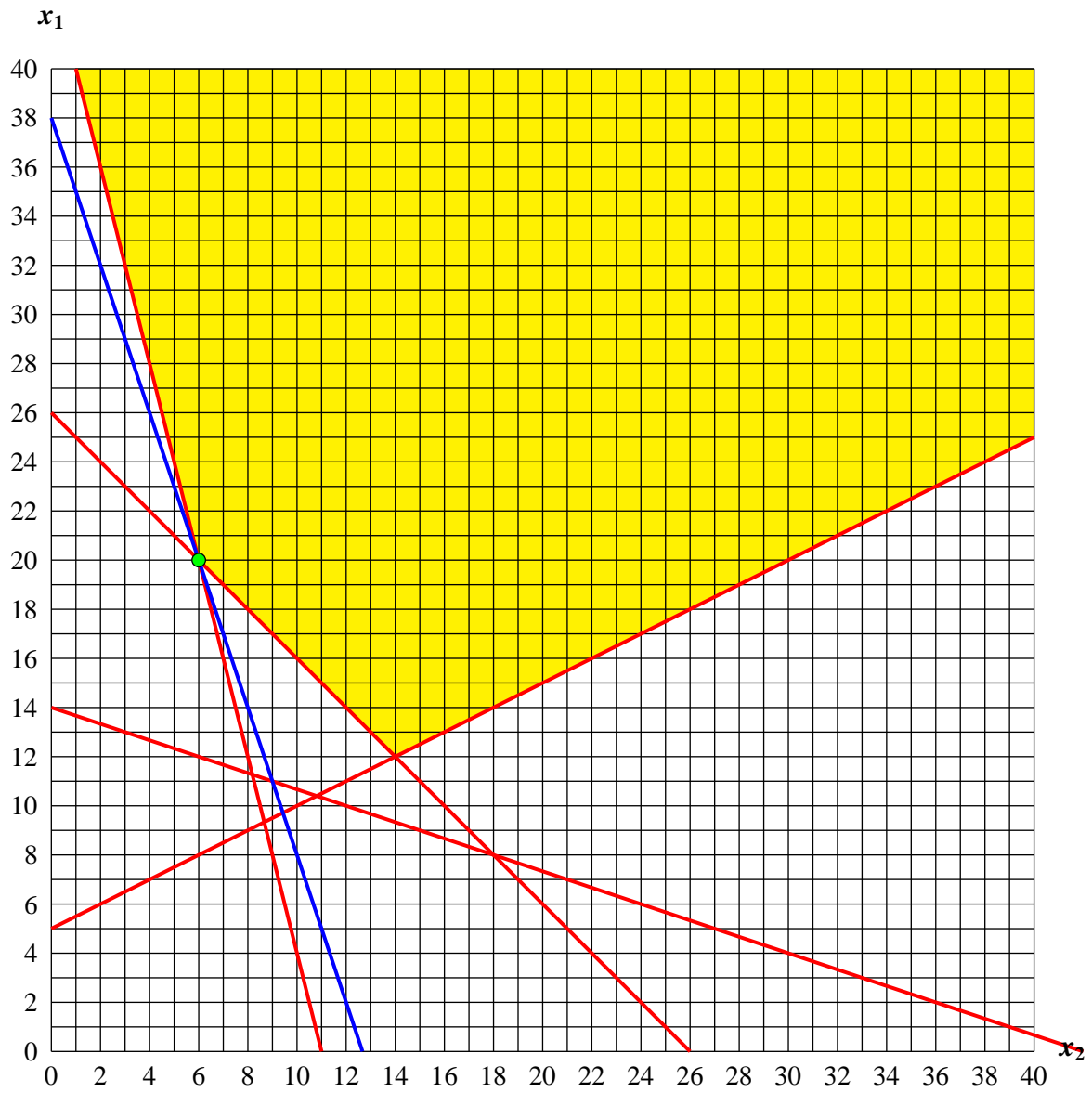
(a) The optimum is $x_1 = 6, x_2 = 12$.

(b) $x_1 = 3, x_2 = 6$.



Question 5 Determine the optimum graphically. *Indicate the feasible set by shading it!*

At an optimum $x_1 = 6, x_2 = 20$



Question 6 **Before-tax demand is $x_1 = 40, x_2 = 0$**

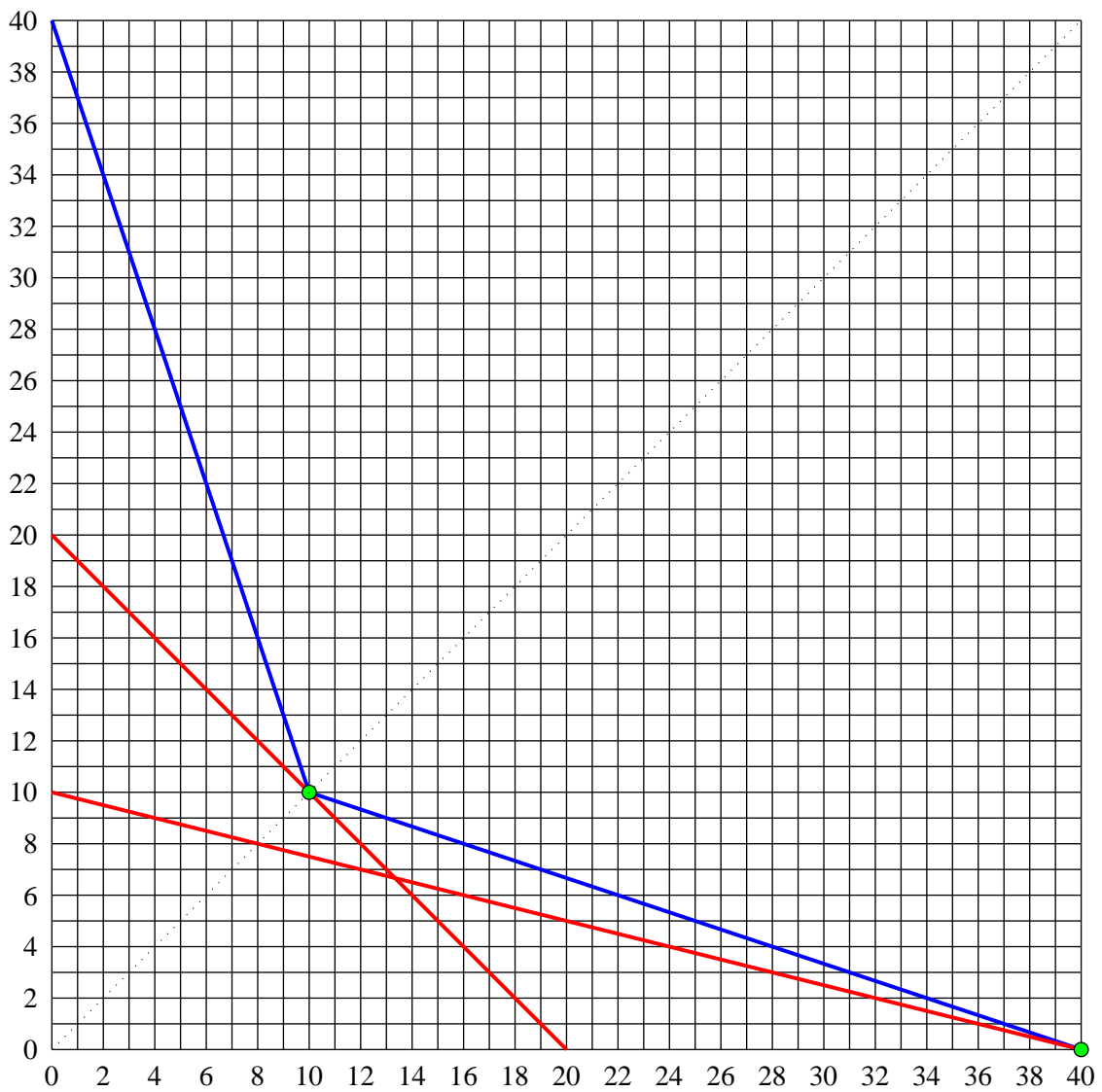
Compensated demand is $x_1 = 10, x_2 = 10$

and the cost of this consumption bundle (at after-tax prices) is 80

which would require a subsidy of 40 to the consumer

After the subsidy is introduced, the government's tax revenue is 30

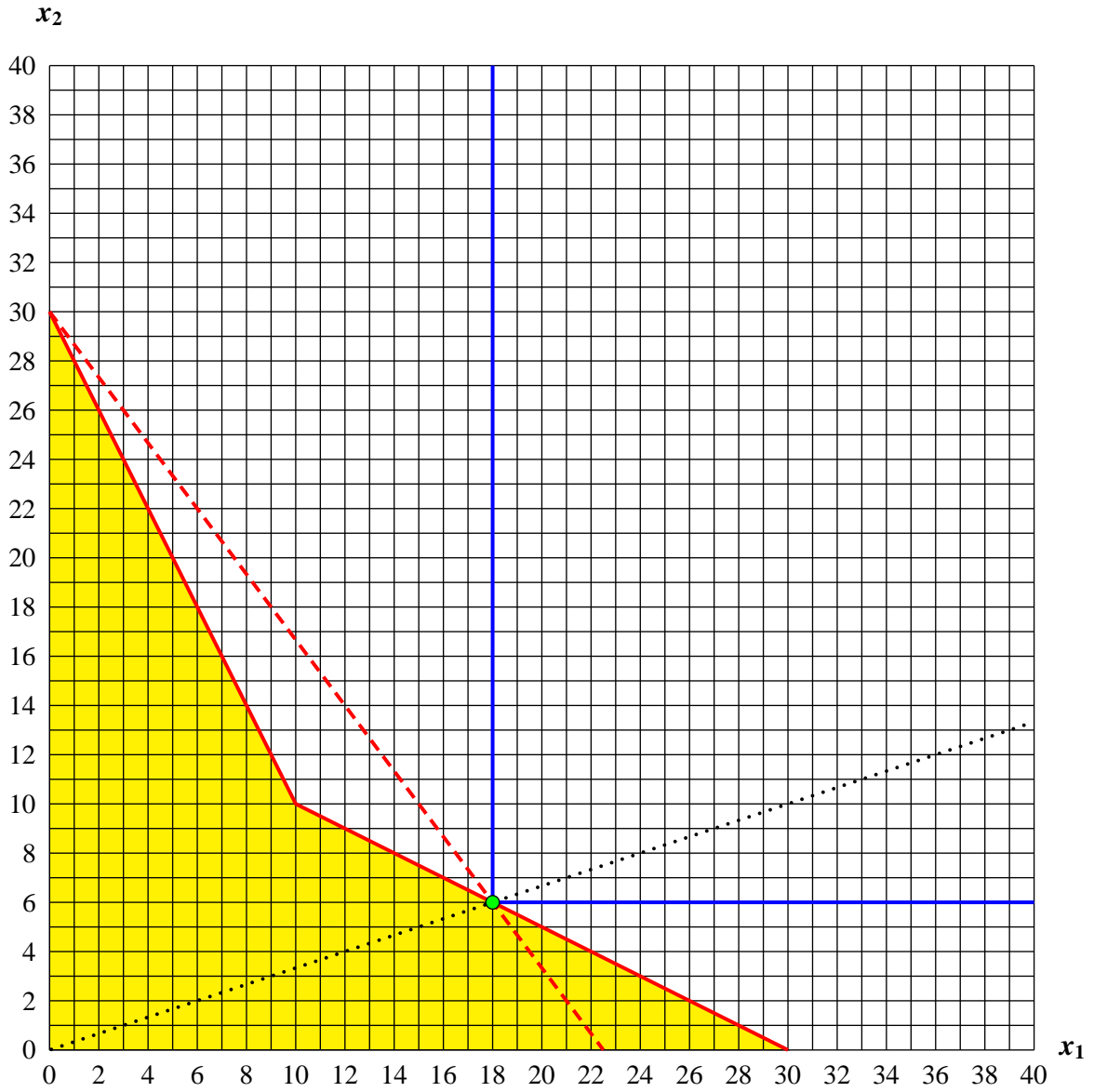
The deadweight loss of the tax is therefore 10



Question 7 **The optimal consumption is $x_1 = 18$ $x_2 = 6$**

At a price of $p'_1 = 2.5$, the person would be able to afford (18, 6) which would be the optimal consumption choice.

$p'_1 = 1.33$



Question 8 Preferences are depicted below.

optimal consumption is $x_1 = 30, x_2 = 0$

The the person needs and income of at least **$I = 81$** .

