# Description

Read, write and extract components of data in Harwell-Boeing sparse matrix format.

# Usage

```
read.matrix.hb(filename)
write.matrix.hb(filename = "hb.out", X, title, key, mxtype, rhs = NULL,
guess = FALSE, xsol = FALSE, ptrfmt = "(16I5)", indfmt = "(16I5)",
valfmt = "(5D16.9)", rhsfmt = "(5D16.9)")
model.matrix(object, ...)
model.response(data)
```

# Arguments

filename	file name to read from or write to
data, object	an object of either matrix.csc.hb or matrix.ssc.hb class
type	One of "any", "numeric", "double". Using the either of latter two coerces the result to have storage mode "double".
X	coefficient matrix stored in csc (for unsymmetric and rectangular matrix) or ssc (for symmetric matrix) format
title	72-character title for the matrix
key	8-character identifier for the matrix
mxtype	3-character identifier for type of the coefficient matrix; First character: currently only "R" for real matrix is supported; second character: "S" for symmetric, "U" for unsymmetric" and "R" for rectangular matrix; third character: currently only "A" for assembled matrix is supported
rhs	vector or matrix of right-hand-side(s) including starting guesses and solution vectors if present stored in full storage mode $$
guess	logical flag for the presence of initial guess of the solutions; if TRUE, the values of initial guess are appended to the end of rhs
xsol	logical flag for the presence of exact solutions; if TRUE, the values of the exact solutions are appended to the end of rhs
ptrfmt	printing format for the column pointers
indfmt	printing format for the row indices
valfmt	printing format for the values
rhsfmt	printing format for the right-hand-sides
• • •	additional arguments

### Details

Sparse coefficient matrices in the Harwell-Boeing format are stored in 80-column records. Each file begins with a multiple line header block followed by two, three or four data blocks. The header block contains summary information on the storage formats and storage requirements. The data blocks contain information of the sparse coefficient matrix and data for the right-hand-side of the linear system of equations, initial guess of the solution and the exact solutions if they exist. The function model.matrix extracts the X matrix component. The function model.response extracts the y vector (or matrix).

#### Value

The function read.matrix.hb returns a list of class matrix.csc.hb or matrix.ssc.hb depending on how the coefficient matrix is stored in the file.

ra	ı	ra component of the csc or ssc format of the coefficient matrix, X.
ja	ì	ja component of the csc or ssc format of the coefficient matrix, X.
ia	ı	ia component of the csc or ssc format of the coefficient matrix, X.
rh	ıs.ra	ra component of the right-hand-side, y, if stored in csc or ssc format; right-hand-side stored in dense vector or matrix otherwise.
rh	ns.ja	ja component of the right-hand-side, y, if stored in $\csc$ or $\sec$ format; a null vector otherwise.
rh	ns.ia	ia component of the right-hand-side, y, if stored in csc or ssc format; a null vector otherwise.
хe	exact	vector of the exact solutions, b, if they exist; a null vector otherwise.
gu	iess	vector of the initial guess of the solutions if they exist; a null vector otherwise.
di	imension	dimenson of the coefficient matrix, X.
rh	ıs.dim	dimenson of the right-hand-side, y.
rh	ns.mode	storage mode of the right-hand-side; can be full storage or same format as the coefficient matrix.

The function model.matrix returns the X matrix of class matrix.csr. The function model.response returns the y vector (or matrix).

# Author(s)

Pin Ng

# References

Duff, I.S., Grimes, R.G. and Lewis, J.G. (1992) User's Guide for Harwell-Boeing Sparse Matrix Collection at http://math.nist.gov/MatrixMarket/collections/hb.html

#### See Also

```
slm for sparse version of lm
SparseM.ops for operators on class matrix.csr
SparseM.solve for linear equation solving for class matrix.csr
SparseM.image for image plotting of class matrix.csr
SparseM.ontology for coercion of class matrix.csr
```

## Examples

```
read.matrix.hb(system.file("HBdata","lsq.rra",package = "SparseM"))-> hb.o
class(hb.o) # -> [1] "matrix.csc.hb"
model.matrix(hb.o)->X
class(X) # -> "matrix.csr"
dim(X) # -> [1] 1850 712
y <- model.response(hb.o) # extract the rhs
length(y) # [1] 1850</pre>
```

SparseM.image

Image Plot for Sparse Matrices

## Description

Display the pattern of non-zero entries of a matrix of class matrix.csr or matrix.csc

# Usage

```
image(x, col=c("white", "gray"), xlab="column", ylab="row", ...)
```

### Arguments

```
    x a matrix of class matrix.csr or matrix.csc.
    col a list of colors such as that generated by 'rainbow'. Defaults to c("white", "gray")
    xlab,ylab each a character string giving the labels for the x and y axis.
    additional arguments.
```

## Details

The pattern of the non-zero entries of a sparse matrix is displayed. By default nonzero entries of the matrix appear as gray blocks and zero entries as white background.

### References

```
Koenker, R and Ng, P. (2002). SparseM: A Sparse Matrix Package for R, http://www.econ.uiuc.edu/~roger/research
```

#### See Also

```
SparseM.ops, SparseM.solve, SparseM.ontology
```

### Examples

```
a <- rnorm(20*5)
A <- matrix(a,20,5)
A[row(A)>col(A)+4|row(A)<col(A)+3] <- 0
b <- rnorm(20*5)
B <- matrix(b,20,5)
B[row(A)>col(A)+2|row(A)<col(A)+2] <- 0
image(as.matrix.csr(A)%*%as.matrix.csr(t(B)))</pre>
```

SparseM.ontology

Sparse Matrix Class

### Description

This group of functions evaluates and coerces changes in class structure.

## Usage

```
as.matrix.csr(x, nrow = 1, ncol = 1, eps = .Machine$double.eps)
as.matrix.csc(x, nrow = 1, ncol = 1, eps = .Machine$double.eps)
as.matrix.ssr(x, nrow = 1, ncol = 1, eps = .Machine$double.eps)
as.matrix.ssc(x, nrow = 1, ncol = 1, eps = .Machine$double.eps)
is.matrix.csr(x, ...)
is.matrix.csc(x, ...)
is.matrix.ssc(x, ...)
```

# Arguments

x is a matrix, or vector object, of either dense or sparse form
nrow number of rows of matrix
ncol number of columns of matrix
eps A tolerance parameter: elements of x such that abs(x) < eps set to zero.
This argument is only relevant when coercing matrices from dense to sparse form. Defaults to eps = .Machine\$double.eps
... other arguments</pre>

#### Details

The function matrix.csc acts like matrix to coerce a vector object to a sparse matrix object of class matrix.csr. The generic functions as.matrix.xxx coerce a matrix x into a matrix of storage class matrix.xxx. The argument matrix x may be of conventional dense form, or of any of the four supported classes: matrix.csr, matrix.csc, matrix.ssr, matrix.ssc. The generic functions is.matrix.xxx evaluate whether the argument is of class matrix.xxx. The function as.matrix transforms a matrix of any sparse class into conventional dense form. The primary storage class for sparse matrices is the compressed sparse row matrix.csr class. An n by m matrix A with real elements  $a_{ij}$ , stored in matrix.csr format consists of three arrays:

ra: a real array of nnz elements containing the non-zero elements of A, stored in row order. Thus, if i < j, all elements of row i precede elements from row j. The order of elements within the rows is immaterial.

ja: an integer array of nnz elements containing the column indices of the elements stored in ra.

ia: an integer array of n+1 elements containing pointers to the beginning of each row in the arrays ra and ja. Thus ia[i] indicates the position in the arrays ra and ja where the *i*th row begins. The last, (n+1)st, element of ia indicates where the n+1 row would start, if it existed.

The compressed sparse column class matrix.csc is defined in an analogous way, as are the matrix.ssr, symmetric sparse row, and matrix.ssc, symmetric sparse column classes.

### Note

as.matrix.ssr and as.matrix.ssc should ONLY be used with symmetric matrices.

#### References

```
Koenker, R and Ng, P. (2002). SparseM: A Sparse Matrix Package for R, http://www.econ.uiuc.edu/~roger/research
```

#### See Also

SparseM.hb for handling Harwell-Boeing sparse matrices.

## Examples

```
n1 <- 10
p <- 5
a <- rnorm(n1*p)
a[abs(a)<0.5] <- 0
A <- matrix(a,n1,p)
B <- t(A)%*%A
A.csr <- as.matrix.csr(A)
A.csc <- as.matrix.csr(A)
B.ssr <- as.matrix.ssr(B)
B.ssc <- as.matrix.ssc(B)
is.matrix.csr(A.csr) # -> TRUE
```

```
is.matrix.csc(A.csc) # -> TRUE
is.matrix.ssr(B.ssr) # -> TRUE
is.matrix.ssc(B.ssc) # -> TRUE
as.matrix(A.csr)
as.matrix(A.csc)
as.matrix(B.ssr)
as.matrix(B.ssc)
as.matrix.csr(rep(0,9),3,3) #sparse matrix of all zeros
```

SparseM.ops

Basic Linear Algebra for Sparse Matrices

### Description

Basic linear algebra operations for sparse matrices of class matrix.csr.

## Usage

```
t(x); diag(x, nrow); diag(x) <- value; ncol(x); nrow(x); dim(x);rbind(...);
cbind(...);x[i,j]; x %*% y; x %% y; x %/% y; x + y; x - y; x * y;
x / y; x ^ y; x > y; x >= y; x < y; x <= y; x == y; x != y; x & y; x | y</pre>
```

### Arguments

```
    x matrix of class matrix.csr.
    y matrix of class matrix.csr or a dense vector.
    value replacement values.
    i,j vectors of elements to extract or replace.
```

nrow optional number of rows for the result.

## Details

Linear algebra operations for matrices of class matrix.csr are designed to behave exactly as for regular matrices. In particular, matrix multiplication, addition, subtraction and various logical operations work as with the conventional dense form of matrix storage, as does indexing, rbind, cbind, and diagonal assignment and extraction.

# References

```
Koenker, R and Ng, P. (2002). SparseM: A Sparse Matrix Package for R, http://www.econ.uiuc.edu/~roger/research
```

### See Also

slm for sparse linear model fitting. SparseM.ontology for coercion and other class relations involving the sparse matrix classes.

## Examples

```
n1 <- 10
n2 <- 10
p <- 6
y <- rnorm(n1)
a <- rnorm(n1*p)
a[abs(a)<0.5] <- 0
A <- matrix(a,n1,p)
A.csr <- as.matrix.csr(A)
b <- rnorm(n2*p)
b[abs(b)<1.0] <- 0
B <- matrix(b,n2,p)
B.csr <- as.matrix.csr(B)</pre>
# matrix transposition and multiplication
A.csr%*%t(B.csr)
```

SparseM.solve

Linear Equation Solving for Sparse Matrices

## Description

chol performs a Cholesky decomposition of a symmetric positive definite sparse matrix x of class matrix.csr.

backsolve performs a triangular back-fitting to compute the solutions of a system of linear equations.

solve combines chol and backsolve and will compute the inverse of a matrix if the right-hand-side is missing.

## Usage

```
chol(x, pivot = FALSE, nsubmax, nnzlmax, tmpmax, ...)
backsolve(r, x, k, upper.tri, transpose)
solve(a, b, ...)
```

## Arguments

a symmetric positive definite matrix of class matrix.csr.

r object of class matrix.csr.chol returned by the function chol.

x,b vector(regular matrix) of right-hand-side(s) of a system of linear equa-

tions.

k inherited from the generic; not used here.

pivot inherited from the generic; not used here.

nsubmax,nnzlmax,tmpmax

dimensions of work arrays, in normal operation these are determined inside the algorithm.

```
upper.tri inherited from the generic; not used here.
transpose inherited from the generic; not used here.
```

... further arguments passed to or from other methods.

#### **Details**

chol performs a Cholesky decomposition of a symmetric positive definite sparse matrix x of class matrix.csr using the block sparse Cholesky algorithm of Ng and Peyton (1993). backsolve does triangular back-fitting to compute the solutions of a system of linear equations. For systems of linear equations that only vary on the right-hand-side, the result from chol can be reused. solve combines chol and backsolve, and will compute the inverse of a matrix if the right-hand-side is missing.

### References

```
Koenker, R and Ng, P. (2002). SparseM: A Sparse Matrix Package for R, http://www.econ.uiuc.edu/~roger/research
```

Ng, E. G. and B. W. Peyton (1993), "Block sparse Cholesky algorithms on advanced uniprocessor computers", SIAM J. Sci. Comput., 14, pp. 1034-1056.

### See Also

slm for sparse version of lm

### Examples

```
# lsq.rra is real rectangular stored in csc (compressed sparse column) format
read.matrix.hb(system.file("HBdata","lsq.rra",package = "SparseM"))-> hb.o
class(hb.o) # -> [1] "matrix.csc.hb"
model.matrix(hb.o)->design.o
class(design.o) # -> "matrix.csr"
dim(design.o) # -> [1] 1850 712
y <- model.response(hb.o) # extract the rhs
length(y) # [1] 1850
t(design.o)%*%design.o -> XpX
t(design.o)%*%design.o -> XpX
t(design.o)%*%y -> Xpy
chol(XpX)->chol.o
backsolve(chol.o,Xpy)-> b1 # least squares solutions in two steps
solve(XpX,Xpy) -> b2 # least squares estimates in one step
```

```
character or NULL-class
```

Class "character or NULL"

## Description

A virtual class needed by the "matrix.csc.hb" class

## Objects from the Class

A virtual Class: No objects may be created from it.

#### Methods

No methods defined with class "character or NULL" in the signature.

lsq

Least Squares Problems in Surveying

## Description

One of the four matrices from the least-squares solution of problems in surveying that were used by Michael Saunders and Chris Paige in the testing of LSQR

# Usage

data(lsq)

#### **Format**

A list of class matrix.csc.hb or matrix.ssc.hb depending on how the coefficient matrix is stored with the following components:

- ra ra component of the csc or ssc format of the coefficient matrix, X.
- ja ja component of the csc or ssc format of the coefficient matrix, X.
- ia ia component of the csc or ssc format of the coefficient matrix, X.
- rhs.ra ra component of the right-hand-side, y, if stored in csc or ssc format; right-hand-side stored in dense vector or matrix otherwise.
- rhs.ja ja component of the right-hand-side, y, if stored in csc or ssc format; a null vector otherwise.
- rhs.ia ia component of the right-hand-side, y, if stored in csc or ssc format; a null vector otherwise.
- xexact vector of the exact solutions, b, if they exist; a null vector o therwise.
- guess vector of the initial guess of the solutions if they exist; a null vector otherwise.
  - dim dimenson of the coefficient matrix, X.
- rhs.dim dimenson of the right-hand-side, y.
- rhs.mode storage mode of the right-hand-side; can be full storage or same format as the coefficient matrix.

#### References

```
Koenker, R and Ng, P. (2002). SparseM: A Sparse Matrix Package for R, http://www.econ.uiuc.edu/~roger/research
Matrix Market, http://math.nist.gov/MatrixMarket/data/Harwell-Boeing/lsq/lsq.html
```

#### See Also

```
read.matrix.hb, write.matrix.hb
```

### Examples

```
data(lsq)
class(lsq) # -> [1] "matrix.csc.hb"
model.matrix(lsq)->X
class(X) # -> "matrix.csr"
dim(X) # -> [1] 1850 712
y <- model.response(lsq) # extract the rhs
length(y) # [1] 1850</pre>
```

matrix.csc-class

Class "matrix.csc"

## Description

A new class for sparse matrices stored in compressed sparse column format

### Objects from the Class

Objects can be created by calls of the form new("matrix.csc", ...).

## Slots

- ra: Object of class "numeric", from class "matrix.csr" a real array of nnz elements containing the non-zero elements of A, stored in row order. Thus, if i<j, all elements of row i precede elements from row j. The order of elements within the rows is immaterial.
- ja: Object of class "numeric", from class "matrix.csr" an integer array of nnz elements containing the column indices of the elements stored in 'ra'.
- ia: Object of class "numeric", from class "matrix.csr" an integer array of n+1 elements containing pointers to the beginning of each row in the arrays 'ra' and 'ja'. Thus 'ia[i]' indicates the position in the arrays 'ra' and 'ja' where the ith row begins. The last, (n+1)st, element of 'ia' indicates where the n+1 row would start, if it existed.
- dimension: Object of class "numeric", from class "matrix.csr" dimension of the matrix

### Extends

Class "matrix.csr", directly.

#### Methods

```
as.matrix.csr signature(x = "matrix.csc"): ...
as.matrix.ssc signature(x = "matrix.csc"): ...
as.matrix.ssr signature(x = "matrix.csc"): ...
as.matrix signature(x = "matrix.csc"): ...
chol signature(x = "matrix.csc"): ...
dim signature(x = "matrix.csc"): ...
t signature(x = "matrix.csc"): ...
```

### See Also

matrix.csr-class

```
matrix.csc.hb-class Class "matrix.csc.hb"
```

## Description

A new class consists of the coefficient matrix and the right-hand-side of a linear system of equations, initial guess of the solution and the exact solutions if they exist stored in external files using the Harwell-Boeing format.

### Objects from the Class

Objects can be created by calls of the form new("matrix.csc.hb", ...).

### Slots

- ra: Object of class "numeric" ra component of the csc or ssc format of the coefficient matrix, X.
- ja: Object of class "numeric" ja component of the csc or s sc format of the coefficient matrix, X.
- ia: Object of class "numeric" ia component of the csc or ssc format of the coefficient matrix, X.
- rhs.ra: Object of class "numeric" ra component of the right-hand-side, y, if stored in csc or ssc format; right-hand-side stored in dense vector or matrix otherwise.
- guess: Object of class "numeric or NULL" vector of the initial guess of the solutions if they exist; a null vector otherwise.
- xexact: Object of class "numeric or NULL" vector of the exact solutions, b, if they exist; a null vector otherwise.
- dimension: Object of class "numeric" dimenson of the coefficient matrix, X.
- rhs.dim: Object of class "numeric" dimenson of the right-hand-side, y.
- rhs.mode: Object of class "character or NULL" storage mode of the right-hand-side; can be full storage or same format as the coefficient matrix.

#### Methods

```
model.matrix signature(object = "matrix.csc.hb"): ...
```

#### See Also

```
model.matrix, model.response, read.matrix.hb, write.matrix.hb, matrix.ssc.hb-
class
```

matrix.csr-class

Class "matrix.csr"

### Description

A new class for sparse matrices stored in compressed sparse row format

### Objects from the Class

Objects can be created by calls of the form new("matrix.csr", ...).

#### Slots

- ra: Object of class "numeric", from class "matrix.csr" a real array of nnz elements containing the non-zero elements of A, stored in row order. Thus, if i<j, all elements of row i precede elements from row j. The order of elements within the rows is immaterial.
- ja: Object of class "numeric", from class "matrix.csr" an integer array of nnz elements containing the column indices of the elements stored in 'ra'.
- ia: Object of class "numeric", from class "matrix.csr" an integer array of n+1 elements containing pointers to the beginning of each row in the arrays 'ra' and 'ja'. Thus 'ia[i]' indicates the position in the arrays 'ra' and 'ja' where the ith row begins. The last, (n+1)st, element of 'ia' indicates where the n+1 row would start, if it existed.
- dimension: Object of class "numeric", from class "matrix.csr" dimension of the matrix

#### Methods

```
%*% signature(x = "matrix.csr", y = "matrix.csr"): ...
%*% signature(x = "matrix.csr", y = "numeric"): ...
as.matrix.csc signature(x = "matrix.csr"): ...
as.matrix.ssc signature(x = "matrix.csr"): ...
as.matrix.ssr signature(x = "matrix.csr"): ...
as.matrix signature(x = "matrix.csr"): ...
chol signature(x = "matrix.csr"): ...
diag signature(x = "matrix.csr"): ...
diag<- signature(x = "matrix.csr"): ...</pre>
```

```
dim signature(x = "matrix.csr"): ...
image signature(x = "matrix.csr"): ...
solve signature(a = "matrix.csr"): ...
t signature(x = "matrix.csr"): ...
```

#### See Also

matrix.csc-class

```
matrix.csr.chol-class

Class "matrix.csr.chol"
```

### Description

A class of objects returned from Ng and Peyton's (1993) block sparse Cholesky algorithm

## Objects from the Class

Objects can be created by calls of the form new("matrix.csr.chol", ...).

#### Slots

```
nrow: Object of class "numeric" number of rows in the linear system of equations
nnzlindx: Object of class "numeric" number of non-zero elements in lindx
nsuper: Object of class "numeric" number of supernodes
lindx: Object of class "numeric" vector of integer containing, in column major order, the
    row subscripts of the non-zero entries in the Cholesky factor in a compressed storage
    format
xlindx: Object of class "numeric" vector of integer of pointers for lindx
nnzl: Object of class "numeric" number of non-zero entries, including the diagonal entries,
    of the Cholesky factor stored in lnz
lnz: Object of class "numeric" contains the entries of the Cholesky factor
xlnz: Object of class "numeric" column pointer for the Cholesky factor stored in lnz
invp: Object of class "numeric" vector of integer of inverse permutation vector
perm: Object of class "numeric" vector of integer of permutation vector
xsuper: Object of class "numeric" array containing the supernode partioning
ierr: Object of class "numeric" error flag
```

### Methods

```
backsolve signature(r = "matrix.csr.chol"): ...
```

time: Object of class "numeric" execution time

## See Also

```
chol, backsolve
```

Class "matrix.ssc"

matrix.ssc-class

## Description

A new class for sparse matrices stored in symmetric sparse column format

## Objects from the Class

Objects can be created by calls of the form new("matrix.ssc", ...).

#### Slots

- ra: Object of class "numeric", from class "matrix.csr" a real array of nnz elements containing the non-zero elements of A, stored in row order. Thus, if i<j, all elements of row i precede elements from row j. The order of elements within the rows is immaterial.
- ja: Object of class "numeric", from class "matrix.csr" an integer array of nnz elements containing the column indices of the elements stored in 'ra'.
- ia: Object of class "numeric", from class "matrix.csr" an integer array of n+1 elements containing pointers to the beginning of each row in the arrays 'ra' and 'ja'. Thus 'ia[i]' indicates the position in the arrays 'ra' and 'ja' where the ith row begins. The last, (n+1)st, element of 'ia' indicates where the n+1 row would start, if it existed.
- dimension: Object of class "numeric", from class "matrix.csr" dimension of the matrix

### Extends

```
Class "matrix.csr", directly.
```

## Methods

```
as.matrix.csc signature(x = "matrix.ssc"): ...
as.matrix.csr signature(x = "matrix.ssc"): ...
as.matrix.ssr signature(x = "matrix.ssc"): ...
as.matrix signature(x = "matrix.ssc"): ...
dim signature(x = "matrix.ssc"): ...
```

### See Also

```
matrix.csr-class
```

## Description

A new class consists of the coefficient matrix and the right-hand-side of a linear system of equations, initial guess of the solution and the exact solutions if they exist stored in external files using the Harwell-Boeing format.

### Objects from the Class

Objects can be created by calls of the form new("matrix.ssc.hb", ...).

#### Slots

- ra: Object of class "numeric" ra component of the csc or ssc format of the coefficient matrix, X.
- ja: Object of class "numeric" ja component of the csc or s sc format of the coefficient matrix, X.
- ia: Object of class "numeric" ia component of the csc or ssc format of the coefficient matrix, X.
- rhs.ra: Object of class "numeric" ra component of the right-hand-side, y, if stored in csc or ssc format; right-hand-side stored in dense vector or matrix otherwise.
- guess: Object of class "numeric or NULL" vector of the initial guess of the solutions if they exist; a null vector otherwise.
- xexact: Object of class "numeric or NULL" vector of the exact solutions, b, if they exist; a null vector otherwise.
- dimension: Object of class "numeric" dimenson of the coefficient matrix, X.
- rhs.dim: Object of class "numeric" dimenson of the right-hand-side, y.
- rhs.mode: Object of class "character or NULL" storage mode of the right-hand-side; can be full storage or same format as the coefficient matrix.

### Extends

```
Class "matrix.csc.hb", directly.
```

#### Methods

```
model.matrix signature(object = "matrix.ssc.hb"): ...
```

### See Also

```
model.matrix, model.response, read.matrix.hb, write.matrix.hb, matrix.csc.hb-
class
```

Class "matrix.ssr"

matrix.ssr-class

## Description

A new class for sparse matrices stored in symmetric sparse row format

# Objects from the Class

Objects can be created by calls of the form new("matrix.ssr", ...).

#### Slots

- ra: Object of class "numeric", from class "matrix.csr" a real array of nnz elements containing the non-zero elements of A, stored in row order. Thus, if i<j, all elements of row i precede elements from row j. The order of elements within the rows is immaterial.
- ja: Object of class "numeric", from class "matrix.csr" an integer array of nnz elements containing the column indices of the elements stored in 'ra'.
- ia: Object of class "numeric", from class "matrix.csr" an integer array of n+1 elements containing pointers to the beginning of each row in the arrays 'ra' and 'ja'. Thus 'ia[i]' indicates the position in the arrays 'ra' and 'ja' where the ith row begins. The last, (n+1)st, element of 'ia' indicates where the n+1 row would start, if it existed.
- dimension: Object of class "numeric", from class "matrix.csr" dimension of the matrix

### Extends

```
Class "matrix.csr", directly.
```

## Methods

```
as.matrix.csc signature(x = "matrix.ssr"): ...
as.matrix.csr signature(x = "matrix.ssr"): ...
as.matrix.ssc signature(x = "matrix.ssr"): ...
as.matrix signature(x = "matrix.ssr"): ...
dim signature(x = "matrix.ssr"): ...
```

### See Also

matrix.csr-class

```
numeric or NULL-class
```

Class "numeric or NULL"

## Description

A virtual class needed by the "matrix.csc.hb" class

## Objects from the Class

A virtual Class: No objects may be created from it.

#### Methods

No methods defined with class "numeric or NULL" in the signature.

slm-class

 $Class\ "slm"$ 

### Description

A sparse extension of 1m

### Objects from the Class

Objects can be created by calls of the form new("slm", ...).

### Slots

```
coefficients: Object of class "numeric" estimated coefficients
chol: Object of class "matrix.csr.chol" Cholesky object from fitting
residuals: Object of class "numeric" residuals
fitted: Object of class "numeric" fitted values
```

### Extends

```
Class "lm", directly. Class "oldClass", by class "lm".
```

### Methods

```
coef signature(object = "slm"): ...
fitted signature(object = "slm"): ...
residuals signature(object = "slm"): ...
summary signature(object = "slm"): ...
```

## See Also

slm

### Description

This is a function to illustrate the use of sparse linear algebra to solve a linear least squares problem using Cholesky decomposition. The syntax and output attempt to emulate lm() but may fails to do so fully satisfactorily. Ideally, this would eventually become a method for lm.

### Usage

```
slm(formula, data, weights, na.action, method = "csr", contrasts = NULL, ...)
```

### Arguments

formula	a formula object,	with the response of	on the left of a $$	operator, and the
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terms, separated by + operators, on the right.

data a data.frame in which to interpret the variables named in the formula,

or in the subset and the weights argument. If this is missing, then the variables in the formula should be on the search list. This may also be a

single number to handle some special cases – see below for details.

weights vector of observation weights; if supplied, the algorithm fits to minimize

the sum of the weights multiplied into the absolute residuals. The length of weights must be the same as the number of observations. The weights must be nonnegative and it is strongly recommended that they be strictly

positive, since zero weights are ambiguous.

na.action a function to filter missing data. This is applied to the model frame after

any subset argument has been used. The default (with na.fail) is to create an error if any missing values are found. A possible alternative is na.omit, which deletes observations that contain one or more missing

values.

method there is only one method based on Cholesky factorization

contrasts a list giving contrasts for some or all of the factors default = NULL appear-

ing in the model formula. The elements of the list should have the same name as the variable and should be either a contrast matrix (specifically, any full-rank matrix with as many rows as there are levels in the factor), or else a function to compute such a matrix given the number of levels.

... additional arguments for the fitting routines

## Value

A list of class slm consisting of:

coefficients estimated coefficients

chol cholesky object from fitting

```
residuals residuals
fitted fitted values
terms terms
call call
```

# Author(s)

Roger Koenker

### References

```
Koenker, R and Ng, P. (2002). SparseM: A Sparse Matrix Package for R, http://www.econ.uiuc.edu/~roger/research
```

### See Also

slm.methods for methods summary, print, fitted, residuals and coef associated with class slm, and slm.fit for lower level fitting functions

### Examples

```
# lsq.rra is real rectangular matrix stored in compressed sparse column format
read.matrix.hb(system.file("HBdata","lsq.rra",package = "SparseM"))-> hb.o
X <- model.matrix(hb.o) #extract the design matrix
y <- model.response(hb.o) # extract the rhs
X1 <- as.matrix(X)
lm.time \leftarrow unix.time(lm(y~X1-1) \rightarrow lm.o) # very slow
cat("slm time =",slm.time,"\n")
cat("slm Results: Reported Coefficients Truncated to 5 ","\n")
sum.slm <- summary(slm.o)</pre>
sum.slm$coef <- sum.slm$coef[1:5,]</pre>
sum.slm
cat("lm time =",lm.time,"\n")
cat("lm Results: Reported Coefficients Truncated to 5 ","\n")
sum.lm <- summary(lm.o)</pre>
sum.lm$coef <- sum.lm$coef[1:5,]</pre>
sum.lm
```

slm.fit

Internal slm fitting functions

## Description

Fitting functions for sparse linear model fitting.

## Usage

```
slm.fit(x,y,method, ...)
slm.wfit(x,y,weights,...)
slm.fit.csr(x, y, ...)
```

### Arguments

x design matrix.

y vector of response observations.

method only csr is supported currently

weights an optional vector of weights to be used in the fitting process. If specified,

weighted least squares is used with weights 'weights' (that is, minimizing

$$\sum w_i * e_i^2$$

... additional arguments.

#### Details

slm.fit and slm.wfit call slm.fit.csr to do Cholesky decomposition and then backsolve to obtain the least squares estimated coefficients. These functions can be called directly if the user is willing to specify the design matrix in matrix.csr form. This is often advantageous in large problems to reduce memory requirements.

## Value

A list of class slm consisting of:

coef estimated coefficients

chol cholesky object from fitting

residuals residuals fitted values

terms terms call

...

## Author(s)

Roger Koenker

### References

```
Koenker, R and Ng, P. (2002). SparseM: A Sparse Matrix Package for R, http://www.econ.uiuc.edu/~roger/research
```

### See Also

slm

 $Methods\ for\ slm\ objects$ 

slm.methods

## Description

Summarize, print, and extract objects from slm objects.

## Usage

# Arguments

object,x	object of class slm.
digits	minimum number of significant digits to be used for most numbers.
symbolic.cor	logical; if TRUE, the correlation of coefficients will be printed. The default is ${\tt FALSE}$
signif.stars	logical; if TRUE, P-values are additionally encoded visually as "significance stars" in order to help scanning of long coefficient tables. It defaults to the 'show.signif.stars' slot of 'options'.
correlation	logical; if TRUE, the correlation matrix of the estimated parameters is returned and printed.
	additional arguments passed to methods.

## Value

print.slm and print.summary.slm return invisibly. fitted.slm, residuals.slm, and coef.slm return the corresponding components of the slm object.

### Author(s)

Roger Koenker

### References

```
Koenker, R and Ng, P. (2002). SparseM: A Sparse Matrix Package for R, http://www.econ.uiuc.edu/~roger/research
```

## See Also

slm

## Examples

```
# lsq.rra is real rectangular matrix stored in compressed sparse column format
read.matrix.hb(system.file("HBdata","lsq.rra",package = "SparseM"))-> hb.o
X <- model.matrix(hb.o) #extract the design matrix
y <- model.response(hb.o) # extract the rhs
X1 <- as.matrix(X)
slm.time <- unix.time(slm(y~X1-1) -> slm.o) # pretty fast
cat("slm time =",slm.time,"\n")
cat("slm Results: Reported Coefficients Truncated to 5 ","\n")
sum.slm <- summary(slm.o)
sum.slm$coef <- sum.slm$coef[1:5,]
sum.slm
fitted(slm.o)[1:10]
residuals(slm.o)[1:10]</pre>
```

summary.slm-class

Class "summary.slm"

### Description

Sparse version of summary.lm

## Objects from the Class

A virtual Class: No objects may be created from it.

### Methods

```
print signature(x = "summary.slm"): ...
```

triogramX

A Design Matrix for a Triogram Problem

## Description

This is a design matrix arising from a bivariate smoothing problem using penalized triogram fitting. It is used in the SparseM vignette to illustrate the use of the sparse matrix image function.

## Usage

```
data(triogramX)
```

### **Format**

A 375 by 100 matrix stored in compressed sparse row format