

This is a Mathematica notebook to illustrate the computations for the welfare analysis of the gasoline demand problem set.  
The long run form of the demand model is:

```
b={-7.733521, 2.798471, -2.53209, -0.21095, 0.6953243}
```

```
q[p_,y_]:=Exp[b[[1]]+b[[2]] Log[y]+b[[3]]Log[p]+b[[4]]Log[p]^2+
           b[[5]]Log[p] Log[y]]
NDSolve[{y'[p]-q[p,y[p]]==0,y[1.3]==15},y,{p,1,5}]
```

Out[6]=

```
{-7.733521, 2.798471, -2.53209, -0.21095, 0.6953243}
```

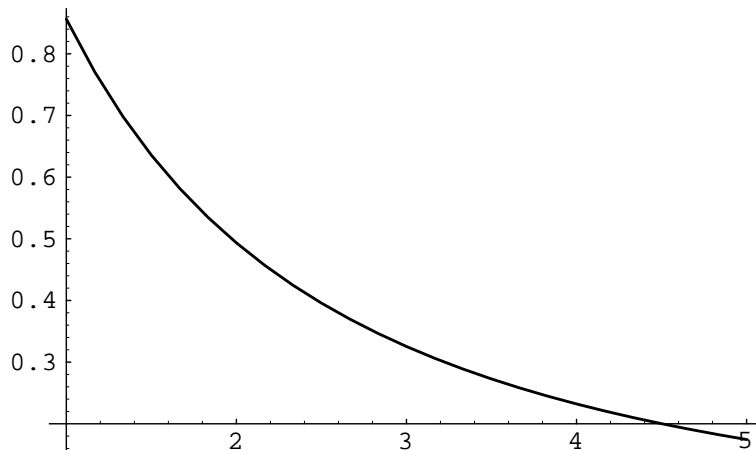
Out[8]=

```
{{y -> InterpolatingFunction[{1., 5.}, <>]}}
```

This is the Marshallian demand curve:

In[9]:=

```
Plot[q[p,15],{p,1,5}]
```

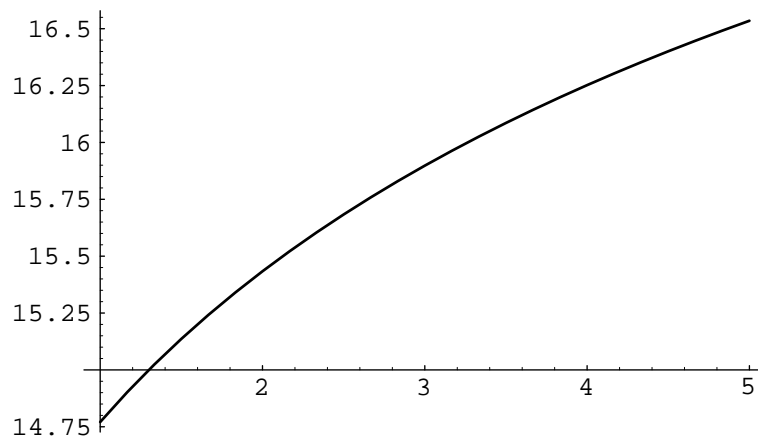


Out[9]=

```
-Graphics-
```

This is the Hicksian equivalent variation or expenditure function obtained by solving the differential equation above

```
Plot[Evaluate[y[p] /. %8],{p,1,5}]
```



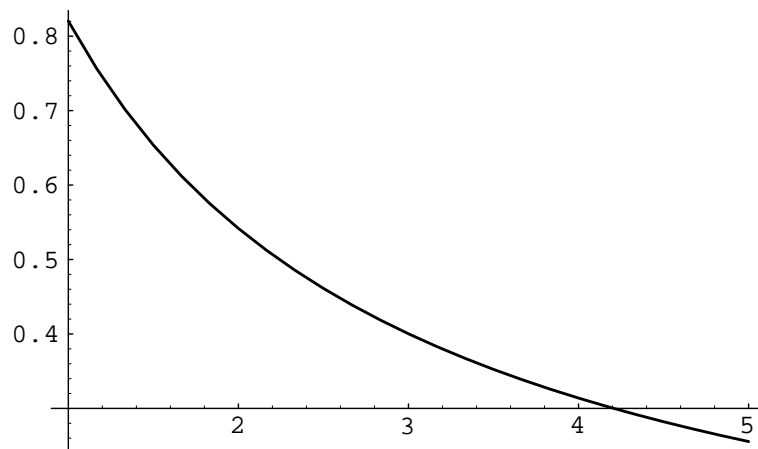
```
Out[10]=
```

```
-Graphics-
```

**This is the Hicksian demand curve**

```
In[11]:=
```

```
Plot[Evaluate[y'[p] /. %8],{p,1,5}]
```

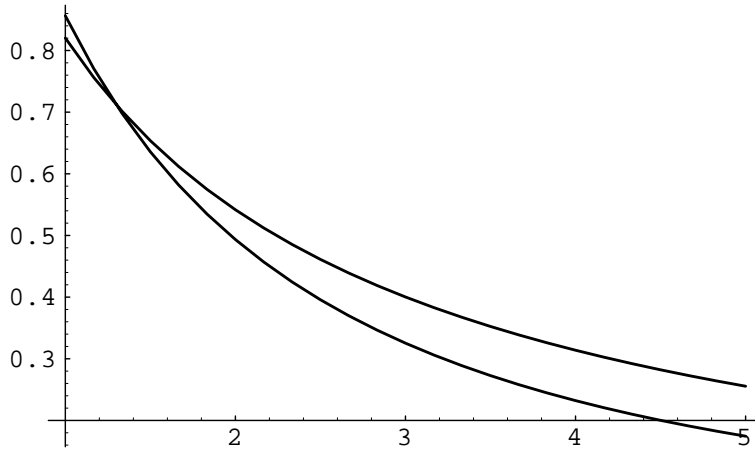


```
Out[11]=
```

```
-Graphics-
```

**This is the Hicksian and Marshallian demand curves superimposed.**

```
In[14]:=
  Show[%11,%9]
```



```
Out[14]=
-Graphics-
```

Now we do several alternative estimates of dead weight loss.

1. Harberger triangle.

```
In[28]:=
  N[1000(1.3-2.)(q[2,15.]-q[1.3,15.])/2]
```

```
Out[28]=
  76.4379
```

2. Integral form of the Harberger triangle.

```
In[33]:=
  1000(NIntegrate[q[p,15],{p,1.3,2.}]- (2.-1.3)q[2.,15.] )
```

```
Out[33]=
  69.0318
```

3. Integral form of Harberger triangle (using Hicksian demand curve).

```
1000(Evaluate[y[2.] /. %8]-Evaluate[y[1.3] /. %8]-(2.-1.3)
      Evaluate[y'[2.] /. %8])
```

Out[32]=

```
{54.36}
```

Note that all of these computations are done for the "representative consumer" with average income -- an interesting extension would be to recompute everything by integrating over the relevant income distribution.